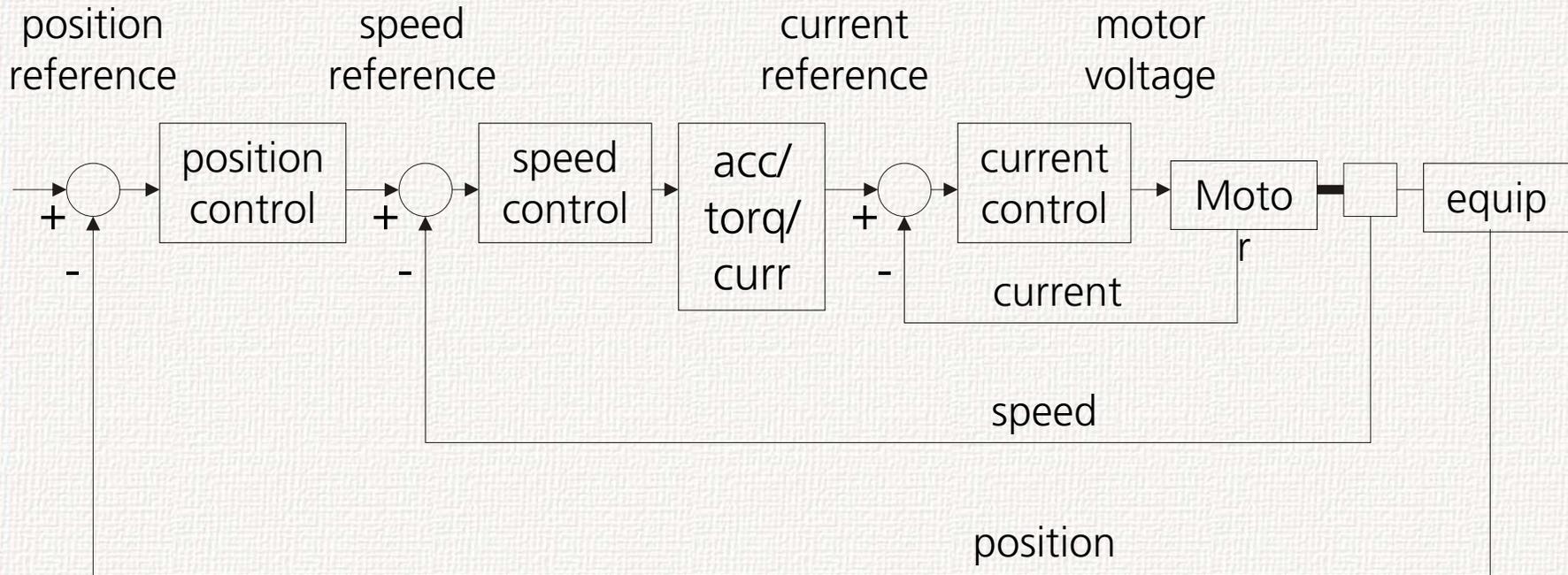


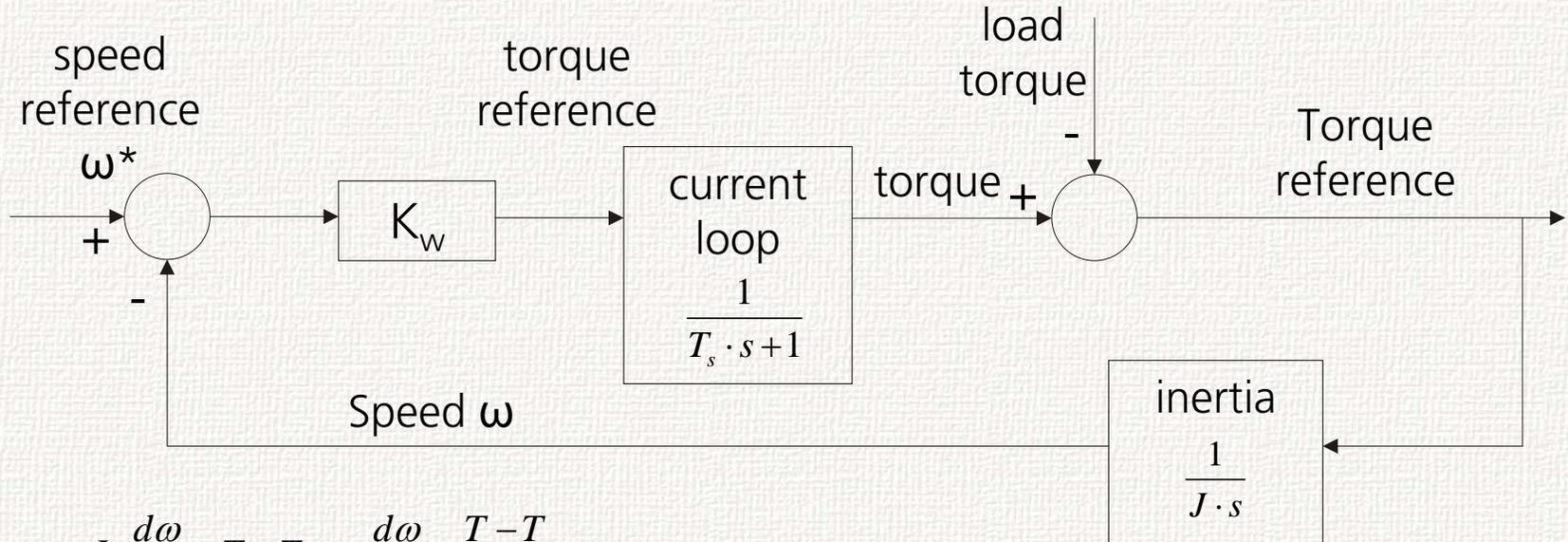
Control



Position control



Speed control



$$J \cdot \frac{d\omega}{dt} = T - T_L \Rightarrow \frac{d\omega}{dt} = \frac{T - T_L}{J}$$

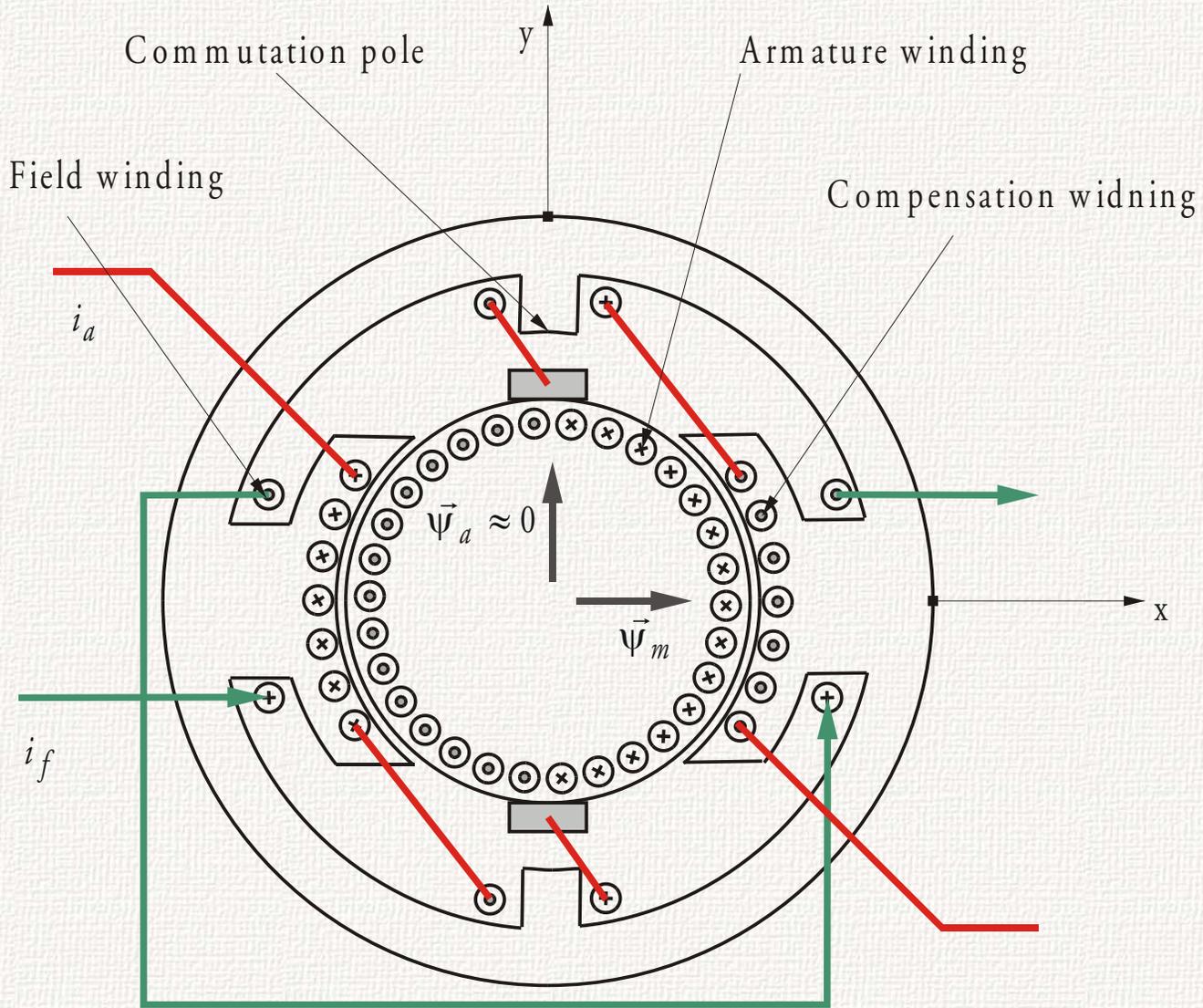
$$\frac{\omega}{\omega^*} = \frac{1}{1 + s \cdot \frac{J}{k_w} + s^2 \cdot \frac{J \cdot T_s}{k_w}}$$

$$s = -\frac{1}{2 \cdot T_s} \pm \sqrt{\left(\frac{1}{2 \cdot T_s}\right)^2 - \frac{k_w}{J \cdot T_s}}$$

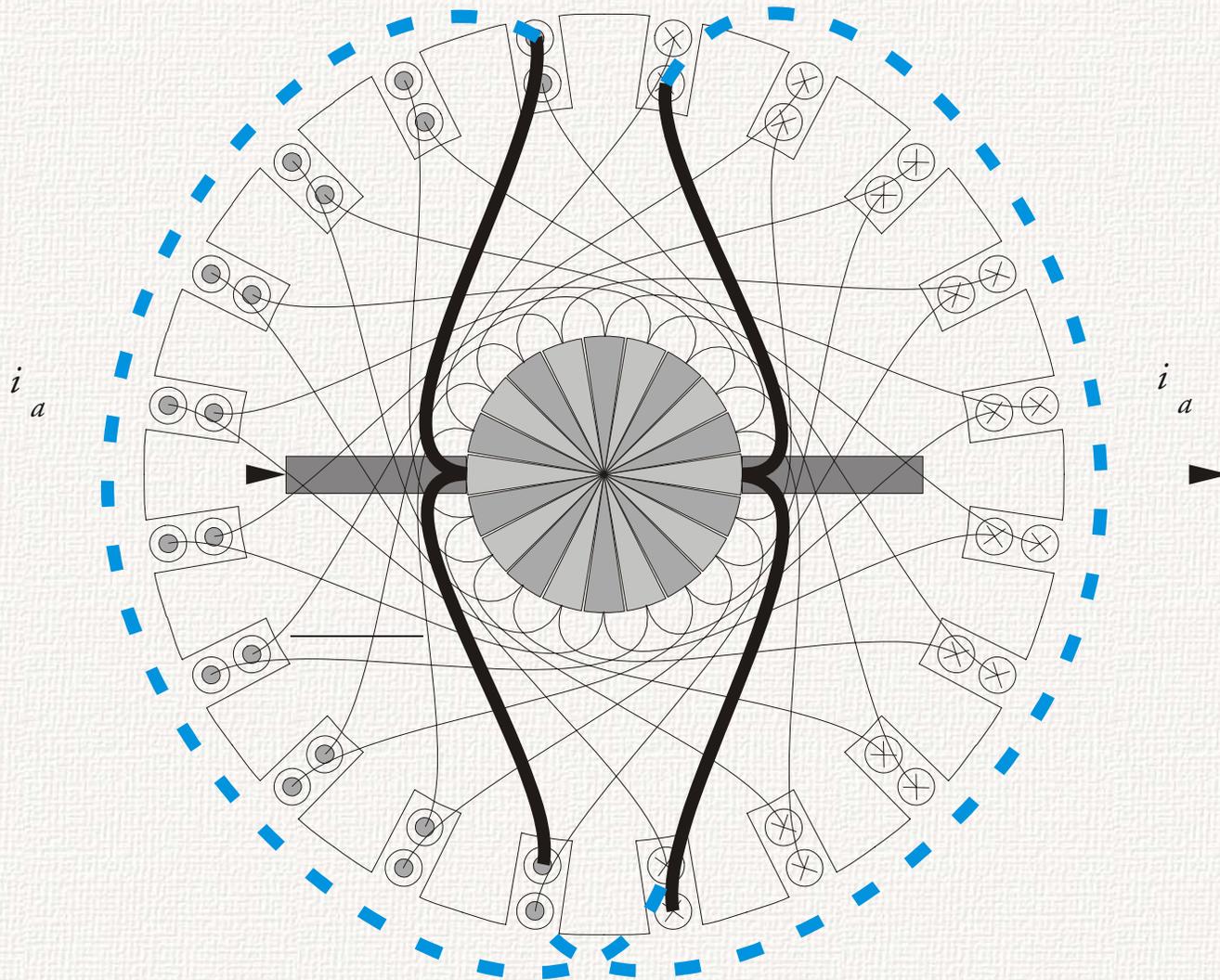
$$k_w = \frac{J}{4 \cdot T_s}$$



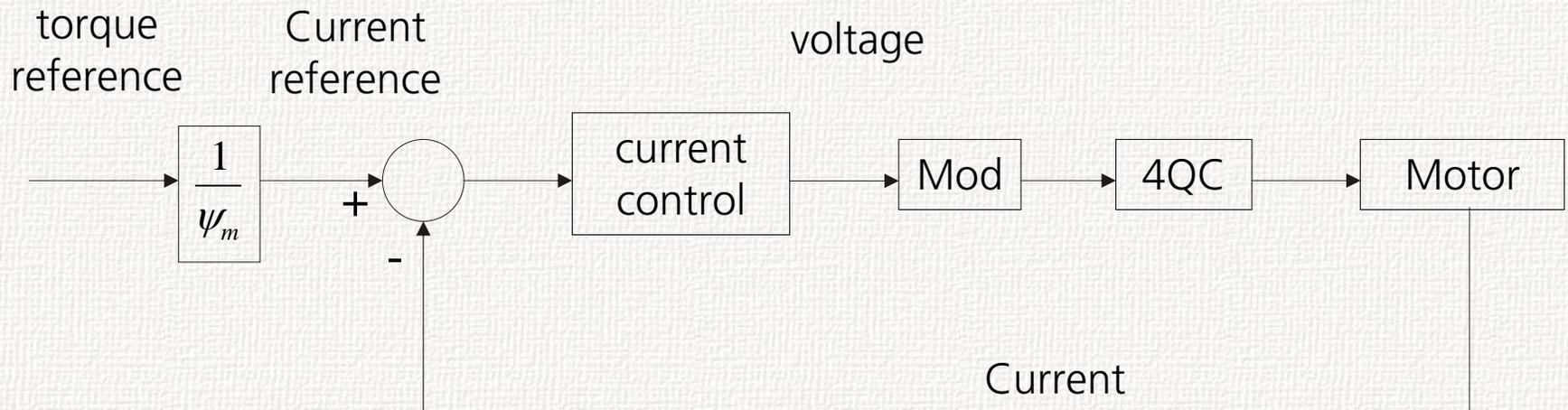
DC-motor



Detailed picture of the rotor



Current control of DC-motor



Current control of DC-motor, cont'd

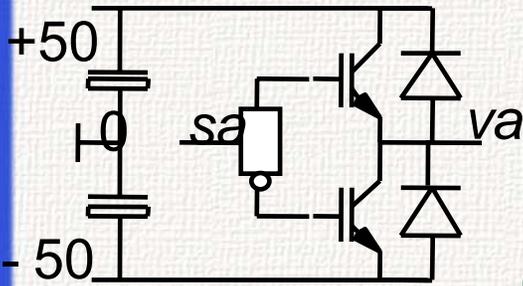
$$u_a = R_a \cdot i_a + L_a \cdot \frac{di_a}{dt} + e_a = \{R_a = 0\} = L_a \cdot \frac{di_a}{dt} + \omega_r \cdot \psi_m$$

$$u_a^*(k) = L_a \cdot \frac{i_a(k+1) - i_a(k)}{T_s} + \omega_r(k) \cdot \psi_m$$

$$u_a^*(k) = k_i \cdot (i_a^*(k) - i_a(k)) + \omega_r(k) \cdot \psi_m$$

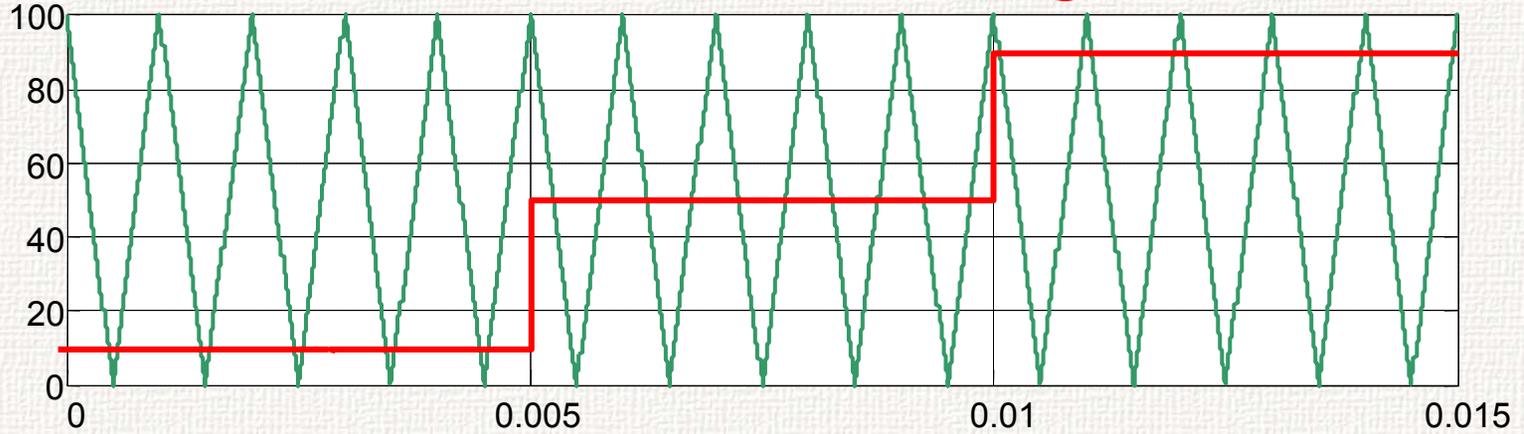


Puls width modulation

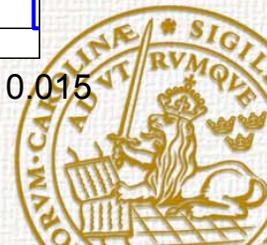
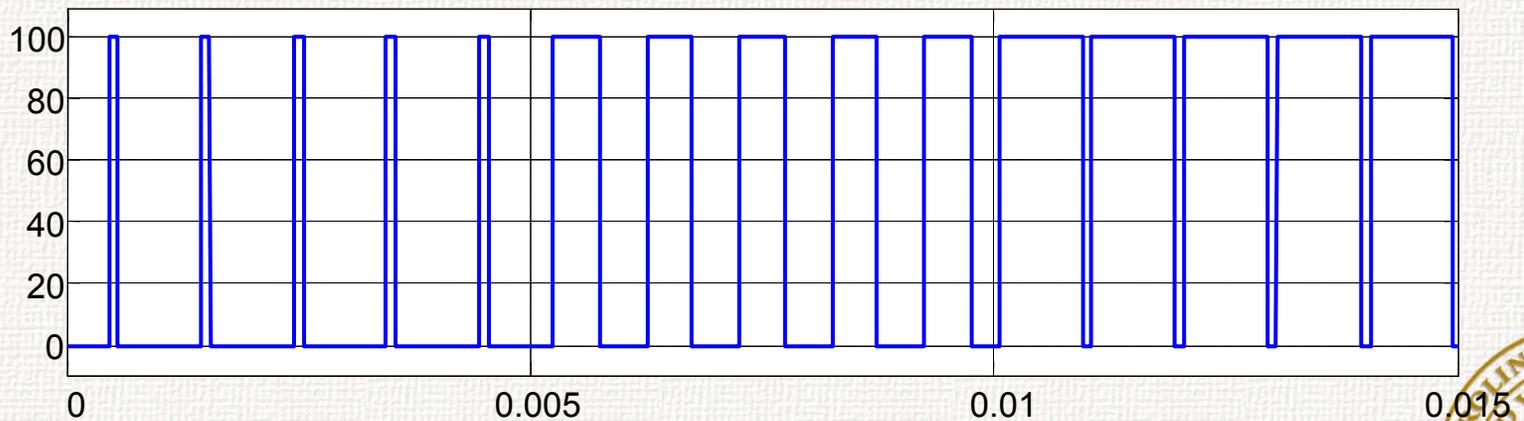


Carrier wave

voltage reference



Output voltage

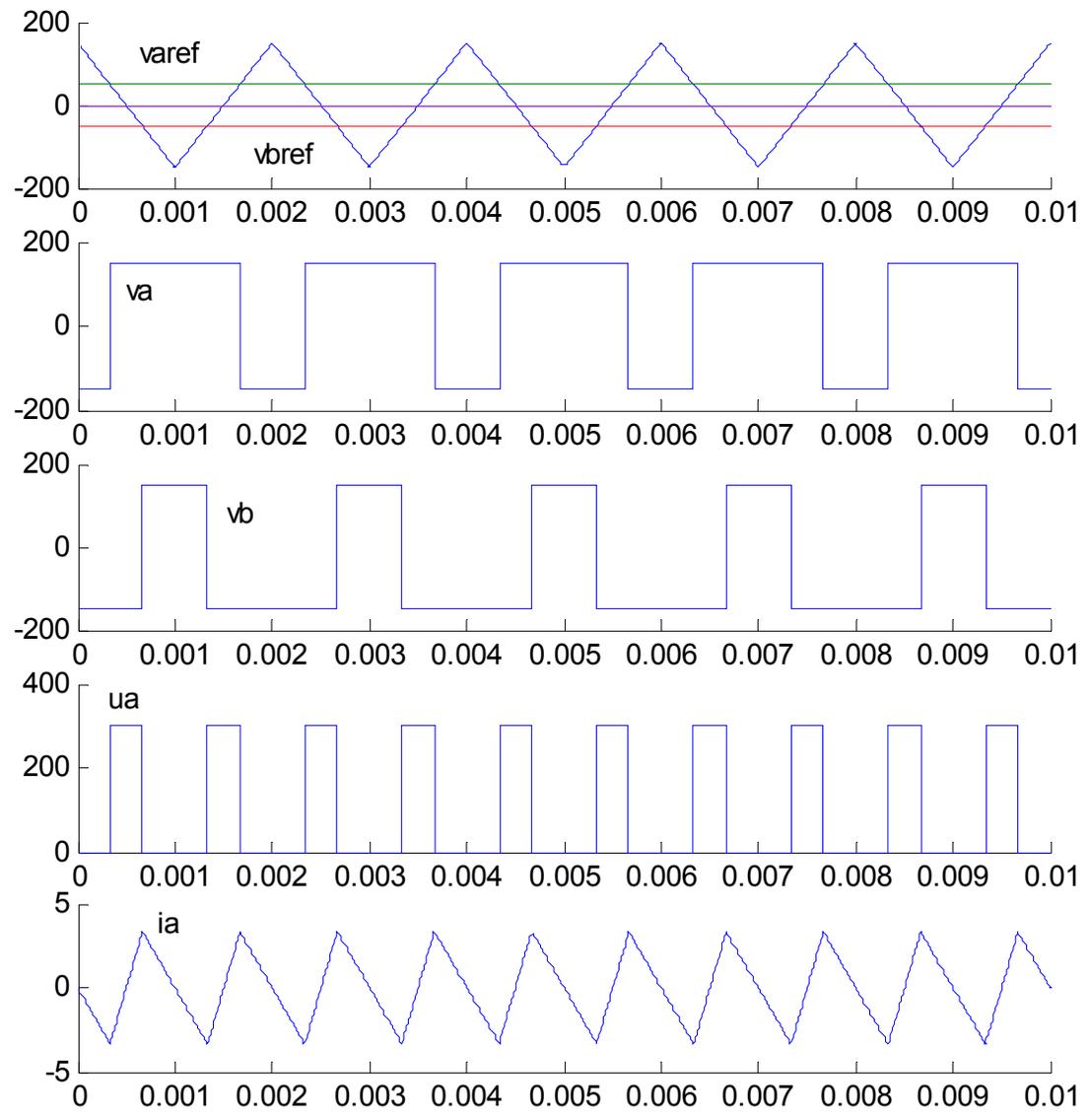


Control of a 4-kv. DC conv:

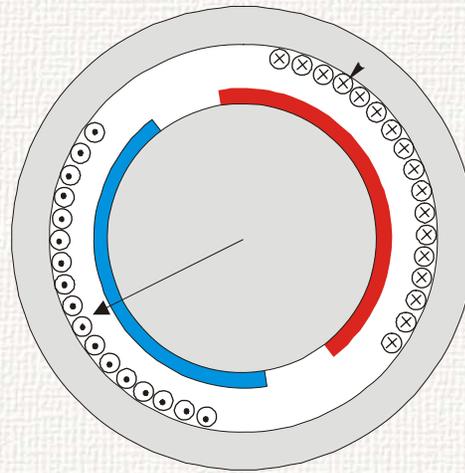
- $v_a^* = u^*/2$
- $v_b^* = -u^*/2$

Example:

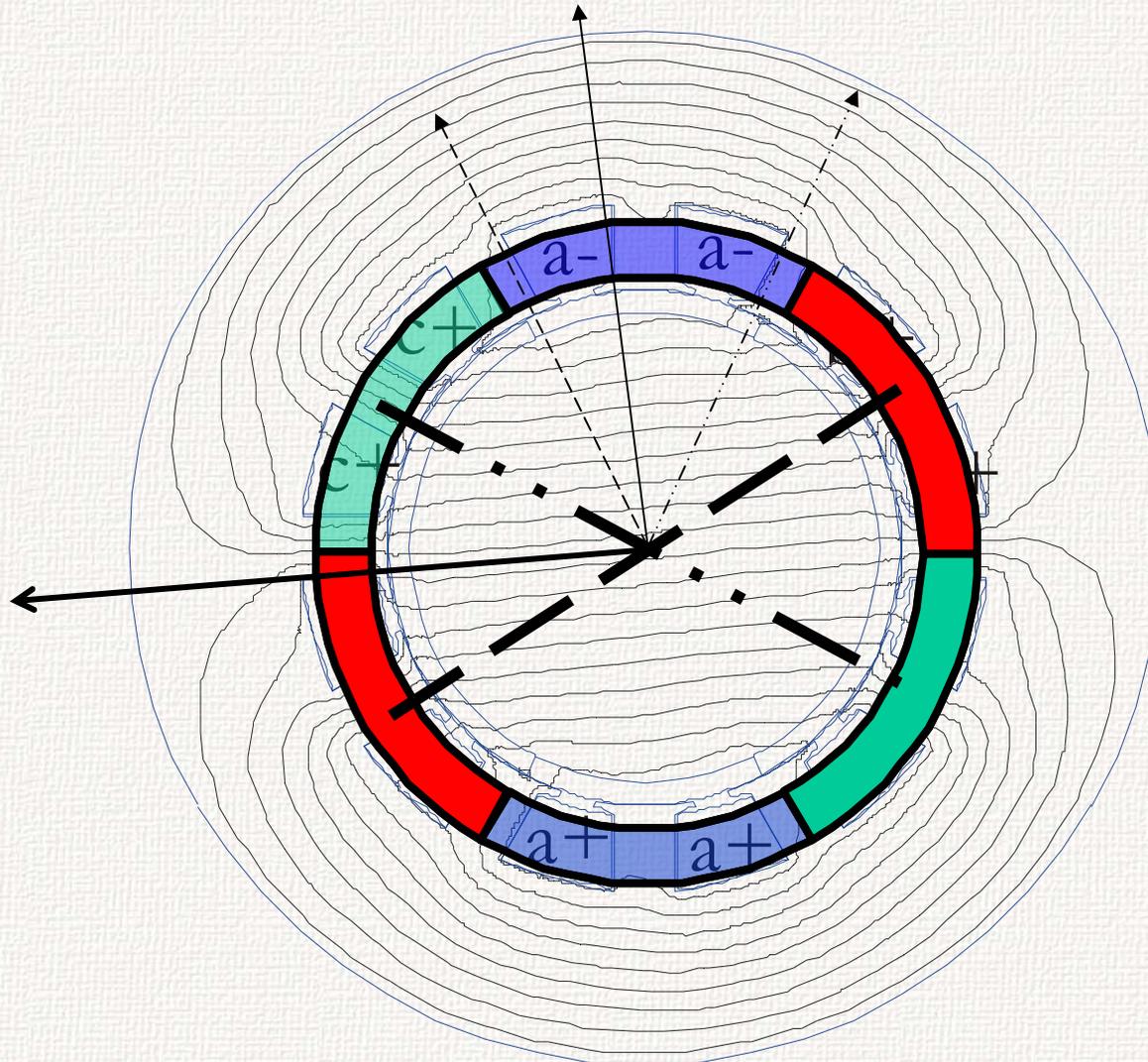
- $U_{dc} = 300\text{ V}$
- $u^* = 100\text{ V}$



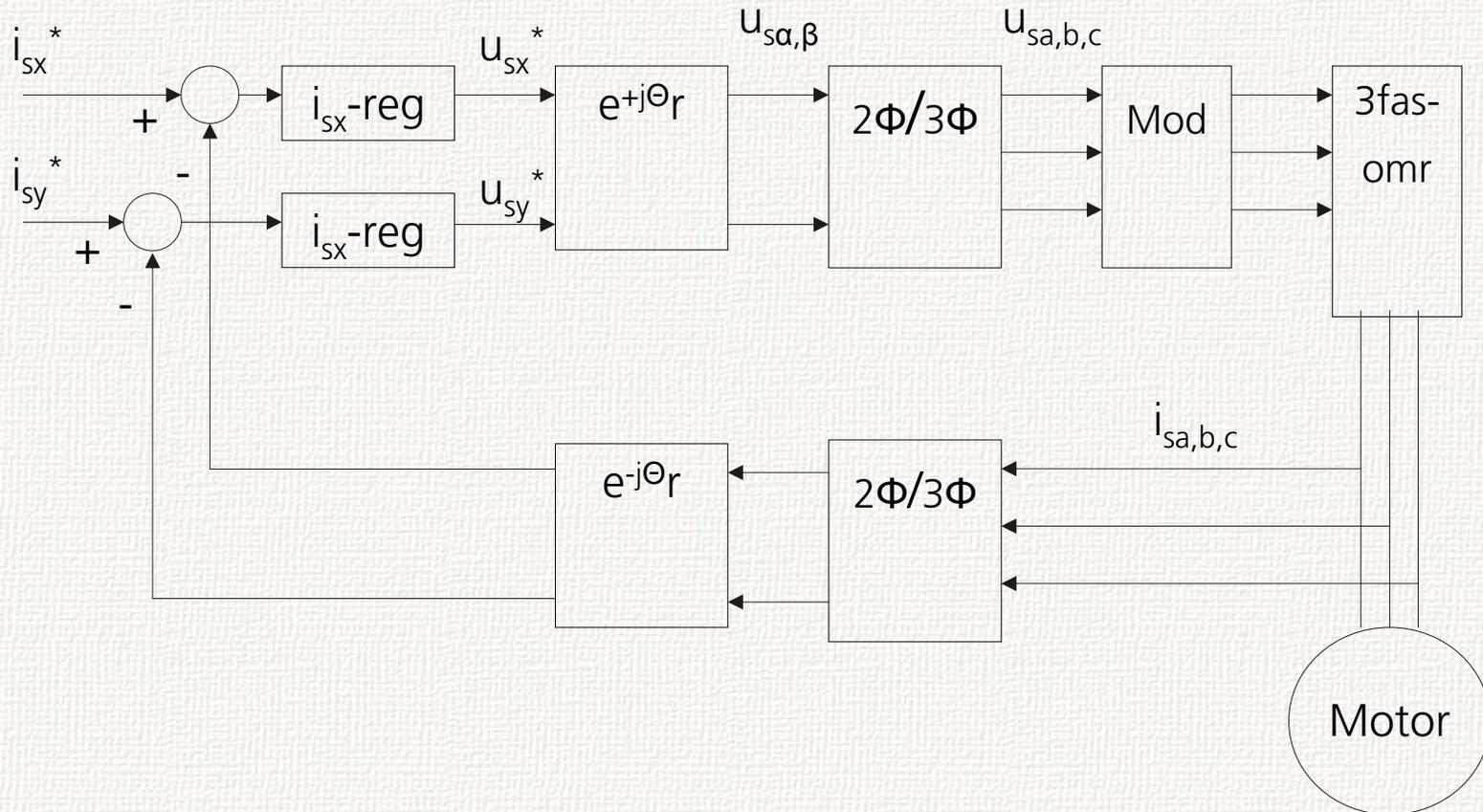
Permanent magnetized synchronous motor, PMSM



3-phase PMSM



Vektor control of a PMSM-motor



Conversion of current from stator to rotor coordinates

$$\begin{aligned}\vec{i}_s^{xy} &= \vec{i}_s^{\alpha\beta} \cdot e^{-j\theta_r} = \vec{i}_s^{\alpha\beta} \cdot e^{-j\omega_r t} = \\ &= \left(i_{s\alpha} \cdot \cos(\omega t) + i_{s\beta} \cdot \sin(\omega t) \right) + j \cdot \left(i_{s\beta} \cdot \cos(\omega t) - i_{s\alpha} \cdot \sin(\omega t) \right)\end{aligned}$$

$$\begin{cases} i_{sx} = i_{s\alpha} \cdot \cos(\omega t) + i_{s\beta} \cdot \sin(\omega t) \\ i_{sy} = i_{s\beta} \cdot \cos(\omega t) - i_{s\alpha} \cdot \sin(\omega t) \end{cases}$$



Current control PMSM

$$\vec{u}_s^* = R_s \cdot \vec{i}_s^* + L_s \cdot \frac{(\vec{i}_s^* - \vec{i}_s)}{T_s} + j\omega \cdot L_s \cdot \vec{i}_s^* + j\omega \cdot \vec{\psi}_m$$

$$\vec{i}_s^* = \frac{T^*}{\psi_m}$$

$$\begin{cases} u_{sx}^* = R_s \cdot i_{sx} + L_s \cdot \frac{(i_{sx}^* - i_{sx})}{T_s} - \omega \cdot L_s \cdot i_{sy} \\ u_{sy}^* = R_s \cdot i_{sy} + L_s \cdot \frac{(i_{sy}^* - i_{sy})}{T_s} + \omega \cdot L_s \cdot i_{sx} + \omega \cdot \psi_m \end{cases}$$

where

$$i_{sx}^* = 0$$

and

$$i_{sy}^* = \frac{T^*}{\psi_m}$$



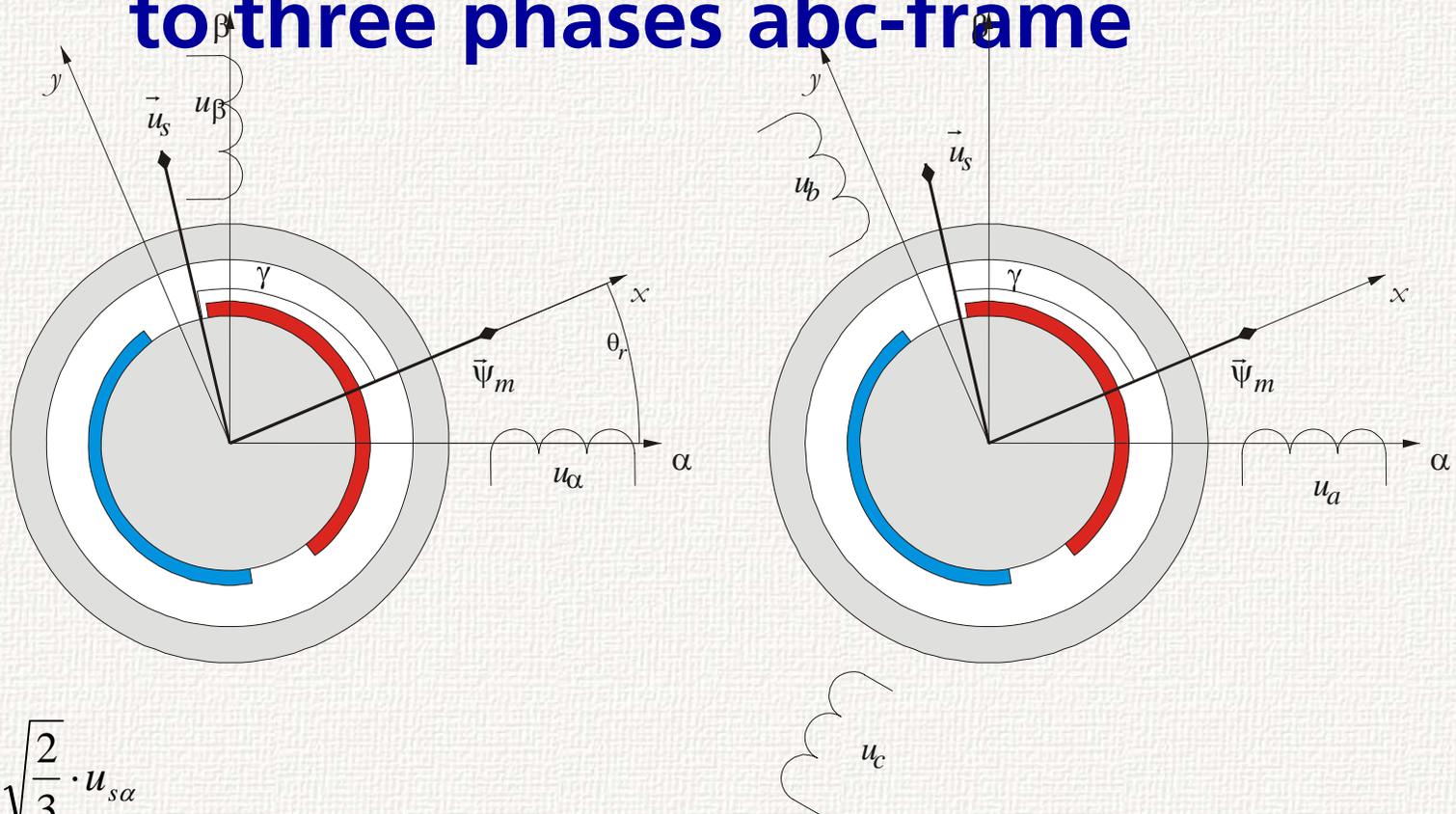
Conversion of stator voltage from rotor to stator coordinates

$$\begin{aligned}\vec{u}_s^{\alpha\beta} &= \vec{u}_s^{xy} \cdot e^{j\theta_r} = \vec{u}_s^{xy} \cdot e^{j\omega_r t} = \\ &= \left(u_{sx} \cdot \cos(\omega t) - u_{sy} \cdot \sin(\omega t) \right) + j \cdot \left(u_{sy} \cdot \cos(\omega t) + u_{sx} \cdot \sin(\omega t) \right)\end{aligned}$$

$$\begin{cases} u_{s\alpha} = u_{sx} \cdot \cos(\omega t) - u_{sy} \cdot \sin(\omega t) \\ u_{s\beta} = u_{sy} \cdot \cos(\omega t) + u_{sx} \cdot \sin(\omega t) \end{cases}$$

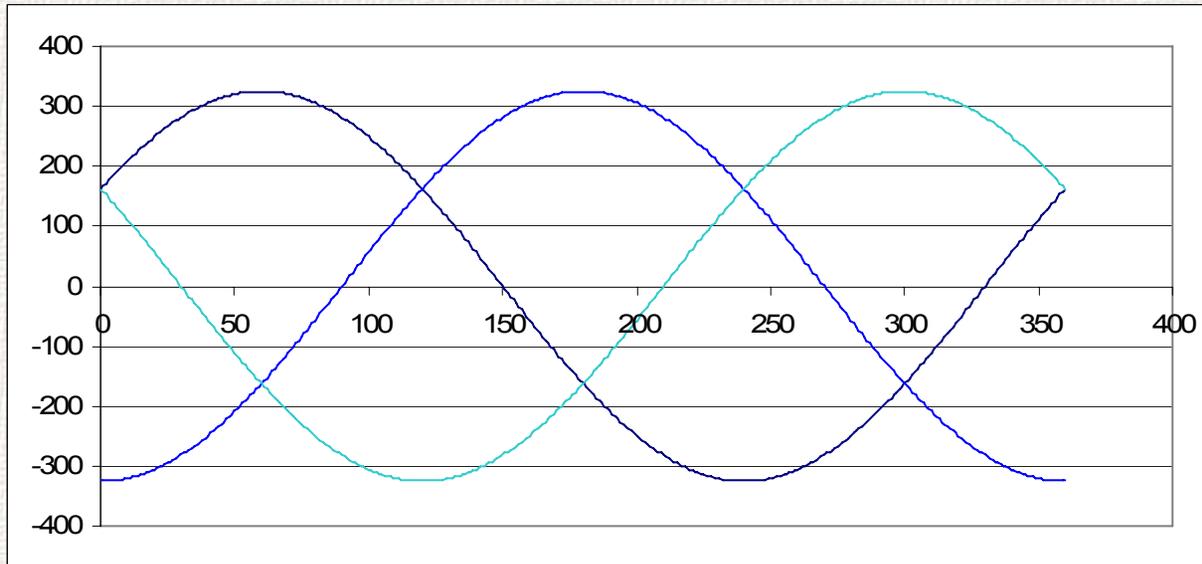


Conversion from two phases $\alpha\beta$ -frame to three phases abc-frame

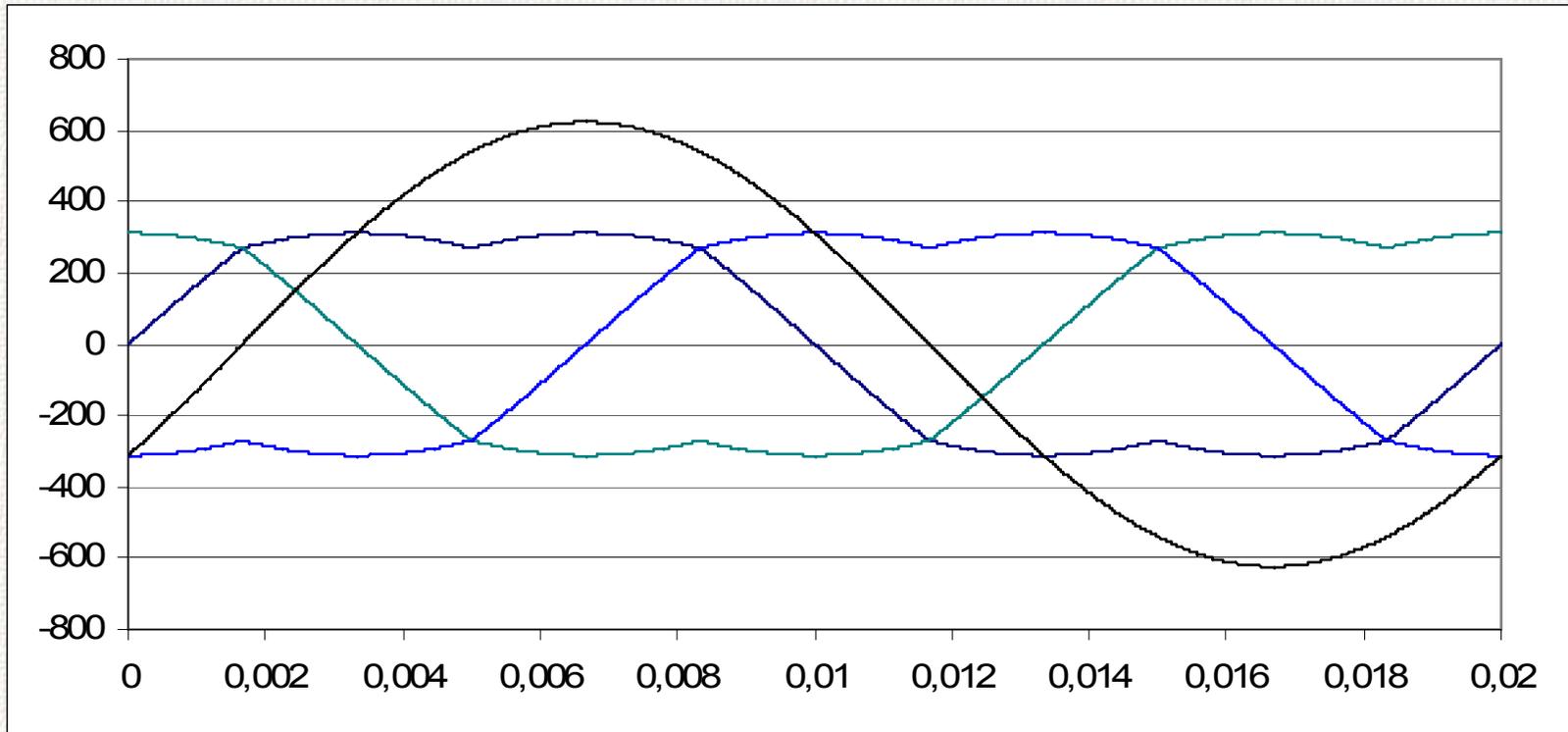


$$\begin{cases} u_a = \sqrt{\frac{2}{3}} \cdot u_{s\alpha} \\ u_b = \sqrt{\frac{2}{3}} \cdot \left(-\frac{1}{2} u_{s\alpha} + \frac{\sqrt{3}}{2} u_{s\beta} \right) \\ u_c = \sqrt{\frac{2}{3}} \cdot \left(-\frac{1}{2} u_{s\alpha} - \frac{\sqrt{3}}{2} u_{s\beta} \right) \end{cases}$$

The 3-phase voltage



Symmetrized motor voltage



Control of 3-phase converter

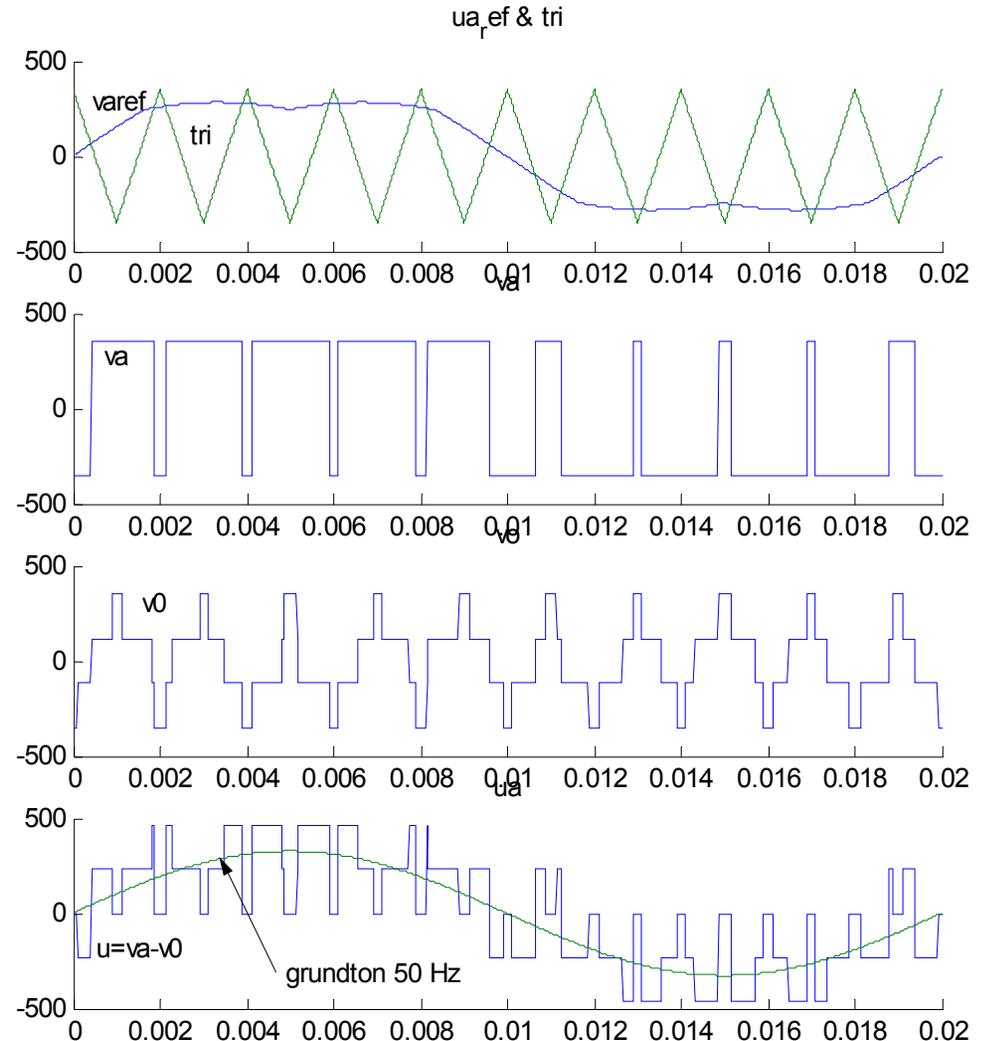
- Symmetrization of references**

$$v_a^* = u_a^* - u_z^*$$

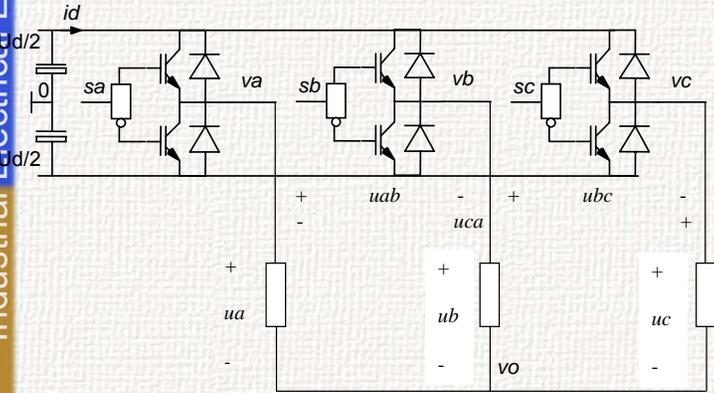
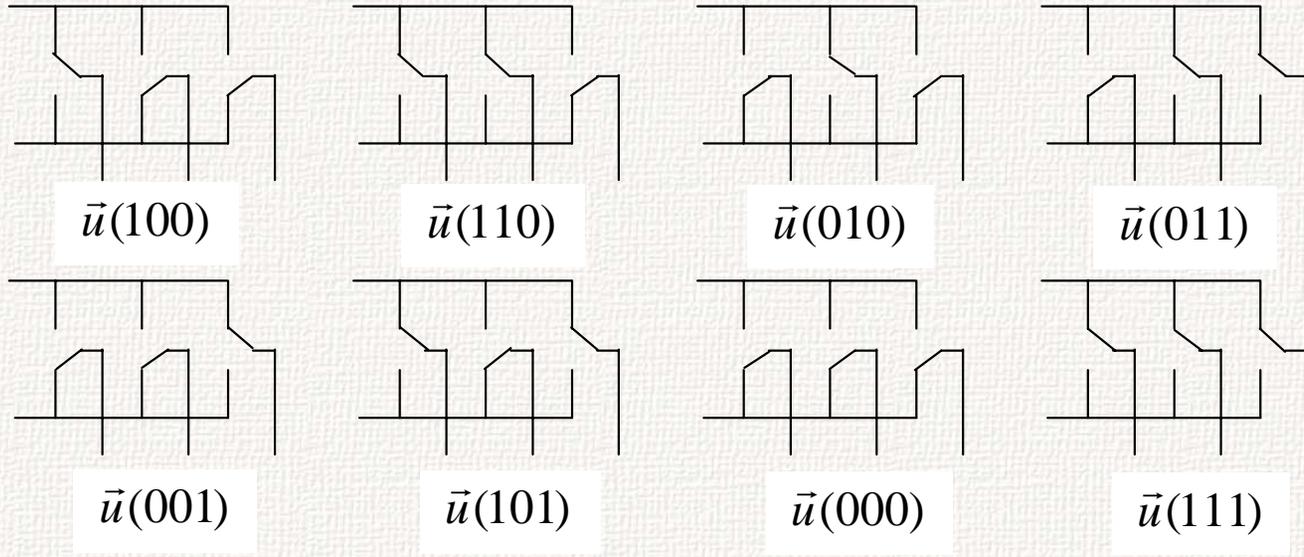
$$v_b^* = u_b^* - u_z^*$$

$$v_c^* = u_c^* - u_z^*$$

$$u_z^* = \frac{\max + \min}{2}$$



3-phase output voltage as vector



$$\vec{u} = u_\alpha + ju_\beta = \sqrt{\frac{2}{3}} \left[u_a + u_b e^{j\frac{2\pi}{3}} + u_c e^{j\frac{4\pi}{3}} \right] = \sqrt{\frac{3}{2}} u_a + j \frac{1}{\sqrt{2}} (u_b - u_c)$$

